

# In a nutshell: Step-by-step optimization

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Given a continuous and differentiable real-valued function  $f$  of a real variable with an initial approximation of an extremum  $x_0$ . This algorithm uses iteration and interpolating polynomials.

Parameters:

$\varepsilon_{\text{step}}$	The maximum error in the value of the minimum cannot exceed this value.
$\varepsilon_{\text{abs}}$	The difference in the value of the function after successive steps cannot exceed this value.
$h$	An initial step size.
$N$	The maximum number of iterations.

1. Let  $k \leftarrow 0$ .
2. If  $k > N$ , we have iterated  $N$  times, so stop and return signalling a failure to converge.
3. Let and letting  $j$  take the values from 1 to  $n$  do the following:
  - a. If  $f(x_k + h) < f(x_k), f(x_k - h)$ , continue calculating  $f(x_k + nh)$  for positive integer values of  $n$  until  $f(x_k + (n+1)h) > f(x_k + nh)$  and then set  $x_{k+1} \leftarrow x_k + nh$ ,
  - b. otherwise, if  $f(x_k - h) < f(x_k), f(x_k + h)$ , continue calculating  $f(x_k - nh)$  for positive integer values of  $n$  until  $f(x_k - (n+1)h) > f(x_k - nh)$  and then set  $x_{k+1} \leftarrow x_k - nh$ ,
  - c. otherwise, set  $x_{k+1} \leftarrow x_k$ .
4. If  $|h| < \varepsilon_{\text{step}}$  and  $|f(x_{k+1}) - \min\{f(x_k - h), f(x_k + h)\}| < \varepsilon_{\text{step}}$ , we are done and return  $x_{k+1}$ .
5. Increment  $k$  and return to Step 2.

Acknowledgement: Jakob Koblinsky noted that I mistakenly copied  $x_{k+1} \leftarrow x_k + nh$  in step 3b, which should be subtracting  $nh$ . This has been corrected.